# A COMPARATIVE STUDY OF FUZZY NEUTROSOPHIC SOFT MATRIX AND ITS DECISION MAKING 

R.Nagarajan*<br>K.Venugopal*


#### Abstract

:

In this paper, we presented fuzzy neutrosophic soft matrices[FNSM] and their operators which are representative of the fuzzy neutrosophic soft sets. The matrix is useful for solving a fuzzy neutrosophic soft set[FNSS] in computer memory which are very useful and applicable. Finally, based on some of the operations on sufficient methodology has been developed to solve FNSS based group decision making problems. Examples are illustrations to verify and compare the proposed algorithms.


Key words: Soft set, Neutrosophic set, Fuzzy neutrosophic soft set, optimal soft set, fuzzy neutrosophic soft matrix, Group decision making.

[^0]1. Introduction: Maji [27], firstly proposed neutrosophic soft sets can handle the indeterminate information and inconsistent information which exists commonly in brief systems. In recent years a number of theories have been proposed to deal with uncertainty, imprecision, Vagueness and indeterminacy. Theory of Probability, fuzzy set theory [44], intuitionistic fuzzy sets [4], interval valued fuzzy sets [3], Vague sets [22], rough set theory [34], neutrosophic theory [37], interval neutrosophic theory [43],etc, are consistently being utilized as efficient tools for diverse types of Uncertainties and impression embedded in a system. However, each of these theories has its inherent difficulties as pointed out by Molodtsov [33], the reason for these difficulties is, possible, the inadequacy of parameterization tool of the theories. The theories has developed in many directions and applied to wide variety of fields such as on soft decision making [12], fuzzy soft decision making [16,17,24,36], on relation of fuzzy soft set [41,42], on relation on neutrosophic soft set [19], on relation on interval valued neutrosophic soft set [18] and so on.

Recently, Cagman et. al [12] introduced soft matrices and applied it in decision making problem. They also introduced fuzzy soft matrices [14], Chetia and Das [11] defined intuitionistic fuzzy soft matrices with different products and properties on these products. Further, Saikia et. al [38] defined generalized fuzzy soft matrices with four different product of generalized intuitionistic fuzzy soft matrices and presented on application in medical diagnosis. Next Broumi et. al [9] studied fuzzy soft matrix based on reference function and defined some new operations such fuzzy soft complement metrics, trace of fuzzy soft matrix based on reference function a new fuzzy soft matrix decision method on reference function is presented.

Recently, Mondal et.al [30,31,32] introduced fuzzy and intuitionistic fuzzy soft matrix and the multicriteria in decision making based on three basic theorem operators. Irfan Deli.et.al. [18] proposed the neutrosophic soft matrices based on decision making,

Our objective is to introduce the concept of FN soft matrices and its applications in decision making problem. The remaining part of this paper is organized us follows. Section 2 contains basic definitions and notations that are used in the remaining parts of the paper. We investigated and defined fuzzy neutrosophic soft set and some operations in Section 3. In section 4, we present group decision making method based on find-product of fuzzy soft neutrosophic matrix. Finally, conclusion is made in section 5.

## 2.Preliminaries

In this section, we give the basic definition and results of Neutrosophic theory (46) soft set theory (39) and soft matrix theory (13) that an useful subsequent discussions.

Definition 2.1: [37]Let $W$ be a space of points (objects), with a generic element in w denote by $u$. A neutrosophic sets ( N -sets) A in w is characterized by a truth-membership function $\mathrm{T}_{\mathrm{A}}$, a indeterminacy membership function $\mathrm{I}_{\mathrm{A}}$ and a falsity-membership function $\mathrm{F}_{\mathrm{A}} . \mathrm{T}_{\mathrm{A}}(\mathrm{w}) ; \mathrm{I}_{\mathrm{A}}(\mathrm{w})$ and $\mathrm{F}_{\mathrm{A}}(\mathrm{w})$ are real standard and non-standard subsets of $[0,1]$. It can be written as $A=\left\{w,<T_{A}(w), \mathrm{I}_{A}(w), \mathrm{F}_{\mathrm{A}}(\mathrm{w})>: \mathrm{w} \in \mathrm{W}, \mathrm{T}_{\mathrm{A}}(\mathrm{w}), \mathrm{I}_{\mathrm{A}}(\mathrm{w}), \mathrm{F}_{\mathrm{A}}(\mathrm{w}) \in[0,1]\right\}$, there is no restriction on the sum of $T_{A}(w), I_{A}(w)$, and $F_{A}(w)$, so $0 \leq \operatorname{Sup} T_{A}(w)+\operatorname{Sup} I_{A}(w)+\operatorname{Sup} F_{A}(w) \leq 3$.

Definition 2.2 :[33] Let $W$ be a Universe, E be a set of parameters that are describe the elements of $w$, and $A \subseteq E$, then a soft set $F_{A}$ over $w$ is a set defined by a set valued function $F_{A}$ representing a mapping $F_{A}: E \rightarrow P(U)$ such that $F_{A}(x)=\phi$ if $x \in E$ where $F_{A}$ is called approximate function of the soft set $\mathrm{F}_{\mathrm{A}}$.

Definition 2.3:[18] Let $\mathrm{W}=\left\{\mathrm{w}_{1}, \mathrm{w}_{2}, \ldots . . \mathrm{w}_{\mathrm{m}}\right\}$ be an initial Universe and then $\left[\mathrm{c}_{\mathrm{i} \phi}\right]=\left[\mathrm{d}_{\mathrm{ij}}\right]$ as in the following way opt ${ }_{[\text {dii] }}(\mathrm{w})=\left\{\mathrm{u}_{\mathrm{i}} / \alpha_{\mathrm{I}}: \mathrm{w}_{\mathrm{i}} \in \mathrm{W}\right\}, \mathrm{d}_{\mathrm{i}}=\max \{\mathrm{s}, \mathrm{y}\}$ which is called an optimum fuzzy set on $w . M_{m m}$ is called Max. min decision function.

Definition 2.4:[18] Let W be the Universe, $\mathrm{N}(\mathrm{w})$ be the set of all neutrosophic sets on W , E be the set of all paramenters that are describe the elements of $W$ and $A \subseteq E$. then, a neutrosophic soft set N over W is a set defined by a set valued function $\mathrm{F}_{\mathrm{N}}$ representing a mapping $\mathrm{F}_{\mathrm{N}}: \mathrm{A} \rightarrow \mathrm{N}(\mathrm{w})$ where $\mathrm{F}_{\mathrm{N}}$ is called approximate function of the neutrosophic soft set N .

Let $\mathrm{N}_{1}$ and $\mathrm{N}_{2}$ be two neutrosophic soft sets over W .

1. $\mathrm{N}_{1}$ is said to be neutrosophic soft subset of $\mathrm{N}_{2}$ if $\mathrm{A}<\mathrm{B}$ and $\mathrm{T}_{\mathrm{FN} 1(\mathrm{x})}(\mathrm{w}) \leq \mathrm{T}_{\mathrm{FN} 2(\mathrm{x})}(\mathrm{w})$, $\mathrm{I}_{\mathrm{FN} 1(\mathrm{x})}(\mathrm{w}) \leq \mathrm{I}_{\mathrm{FN} 2(\mathrm{x})}(\mathrm{w}), \mathrm{F}_{\mathrm{FN} 1(\mathrm{x})}(\mathrm{w}) \geq \mathrm{F}_{\mathrm{FN} 2(\mathrm{x})}(\mathrm{w})$, for all $\mathrm{x} \in \mathrm{A}, \mathrm{w} \in \mathrm{W}$.
2. $\mathrm{N}_{1}$ and $\mathrm{N}_{2}$ are said to be equal if $\mathrm{N}_{1}$ neutrosophic soft subset of $\mathrm{N}_{2}$ and $\mathrm{N}_{2}$ neutrosophic soft set of $\mathrm{N}_{1}$.

Definition 2.5: A fuzzy subset of a nonempty set $X$ is defined as a function $\mu: X \rightarrow[0,1]$.

Definition 2.6: Let $W$ be the initial Universal set and $E$ be a set of parameters. Let $P(W)$ denote the set of all fuzzy neutrosophic set of W. Consider a non-empty set A, A C E. The collection $(F, A)$ is termed to be the 'fuzzy neutrosophic soft' set over W , where $\mathrm{F}: \mathrm{A} \rightarrow \mathrm{P}(\mathrm{W})$. It is denoted by FNSS.

Let $\mathrm{N}_{1}$ and $\mathrm{N}_{2}$ be two fuzzy neutrosophic soft sets. Then

Complement $\mathrm{N}_{1}{ }^{\mathrm{c}}=\left\{\left(\mathrm{x},\left\{<\mathrm{u}, \mathrm{F}_{\mathrm{FNl}(\mathrm{x})}(\mathrm{w}), \mathrm{I}_{\mathrm{FNl}(\mathrm{x})}(\mathrm{w}), \mathrm{T}_{\mathrm{FNl}(\mathrm{x})}(\mathrm{w})>: \mathrm{x} \in \mathrm{W}, \mathrm{x} \in \mathrm{E}\right\}\right.\right.$.
Union N1 U N2 $=\left\{\left(x,\left\{w, T_{\text {N1UN2 }}(w), I_{\text {N1UN2 }}(w), F_{\text {N1UN2 }}(w)>: x \in W, x \in E\right\}\right.\right.$

Intersection $\mathrm{N} 1 \cap \mathrm{~N} 2=\left\{\left(\mathrm{x},\left\{\mathrm{w}, \mathrm{T}_{\mathrm{N} 1} \cap_{\mathrm{N} 2}(\mathrm{w}), \mathrm{I}_{\mathrm{N} 1} \cap_{\mathrm{N} 2}(\mathrm{w}), \mathrm{F}_{\mathrm{N} 1} \cap_{\mathrm{N} 2}(\mathrm{w})>: \mathrm{x} \in \mathrm{W}, \mathrm{x} \in \mathrm{E}\right\}\right.\right.$.

## Example :

Let $W=\left\{w_{1}, w_{2}, W_{3}, w_{4}\right\}, E=\left\{e_{1}, e_{2}, e_{3}\right\} . N_{1}$ and $N_{2}$ be two fuzzy neutrosophic soft sets as
$\mathrm{N}_{1}=\left\{\left(\mathrm{e}_{1},\left\{\left\langle\mathrm{w}_{1},(0.4 \mathbf{I}, 0.5,0.8)\right\rangle,\left\langle\mathrm{w}_{2},(0.2,0.5 \mathbf{I}, 0.1 \mathrm{I})\right\rangle,\left\langle\mathrm{w}_{3},(0.3,0.1 \mathbf{I}, 0.4)\right\rangle,\left\langle\mathrm{w}_{4},(0.4,0.7\right.\right.\right.\right.$, $0.7 \mathbf{I})\rangle\}), \mathrm{e}_{2},\left\{\left\langle\mathrm{w}_{1},(0.5 \mathbf{I}, 0.7,0.7)\right\rangle,\left\langle\mathrm{w}_{2},(0.3,0.6 \mathbf{I}, 0.3)\right\rangle,\left\langle\mathrm{w}_{3},(0.2 \mathbf{I}, 0.6,0.5)\right\rangle,\left\langle\mathrm{w}_{4},(0.4\right.\right.$, $0.5 \mathbf{I}, 0.5)\rangle\}),\left\{\mathrm{e}_{3},\left\{\left\langle\mathrm{w}_{1},(0.7,0.8 \mathbf{I}, 0.6 \mathrm{I})\right\rangle,\left\langle\mathrm{w}_{2},(0.5 \mathrm{I}, 0.6,0.7 \mathrm{I})\right\rangle,\left\langle\mathrm{w}_{3},(0.7 \mathrm{I}, 0.5,0.8)\right\rangle,\left\langle\mathrm{w}_{4},(0.2 \mathrm{I}\right.\right.\right.$, $0.8,0.5)>$ ) \}
$\mathrm{N}_{2}=\left\{\left(\mathrm{e}_{1},\left\{\left\langle\mathrm{w}_{1},(0.7 \mathrm{I}, 0.6,0.7)\right\rangle,\left\langle\mathrm{w}_{2},(0.4,0.2 \mathrm{I}, 0.8)\right\rangle,\left\langle\mathrm{w}_{3},(0.9,0.1,0.5 \mathrm{I})\right\rangle,\left\langle\mathrm{w}_{4},(0.4 \mathrm{I}, 0.7\right.\right.\right.\right.$, $0.7 \mathrm{I})\rangle\}),\left\{\mathrm{e}_{2},\left\{\left\langle\mathrm{w}_{1},(0.5,0.7 \mathrm{I}, 0.8)\right\rangle,\left\langle\mathrm{w}_{2},(0.5,0.9 \mathrm{I}, 0.3)\right\rangle,\left\langle\mathrm{w}_{3},(0.5 \mathrm{I}, 0.6,0.8)\right\rangle,\left\langle\mathrm{w}_{4},(0.5\right.\right.\right.$, $0.8 \mathrm{I}, 0.5)\rangle\}),\left\{\mathrm{e}_{3},\left\{\left\langle\mathrm{w}_{1},(0.8 \mathrm{I}, 0.6,0.9 \mathrm{I})\right\rangle,\left\langle\mathrm{w}_{2},(0.5,0.9 \mathrm{I}, 0.9)\right\rangle,\left\langle\mathrm{w}_{3},(0.7,0.5 \mathrm{I}, 0.4)\right\rangle,\left\langle\mathrm{w}_{4},(0.3 \mathrm{I}\right.\right.\right.$, $0.5,0.6 \mathrm{I})>$ ) $\}$

Then

N1UN2 $=\left\{\left(\mathrm{e}_{1},\left\{\left\langle\mathrm{w}_{1},(0.7 \mathrm{I}, 0.5,0.7)\right\rangle,\left\langle\mathrm{W}_{2},(0.4,0.2 \mathrm{I}, 0.1 \mathrm{I})\right\rangle,\left\langle\mathrm{W}_{3},(0.9,0.1 \mathrm{I}, 0.4)\right\rangle,\left\langle\mathrm{w}_{4},(0.4 \mathrm{I}, 0.2 \mathrm{I}\right.\right.\right.\right.$, $0.5)\rangle),\left(\mathrm{e}_{2},\left\{\left\langle\mathrm{w}_{1},(0.5,0.7,0.7)\right\rangle,\left\langle\mathrm{w}_{2},(0.5,0.2 \mathrm{I}, 0.3)\right\rangle,\left\langle\mathrm{w}_{3},(0.5 \mathrm{I}, 0.6,0.5)\right\rangle,\left\langle\mathrm{w}_{4},(0.5,0.5 \mathrm{I}\right.\right.\right.$, $0.5)\rangle),\left(e_{3},\left\{\left\langle w_{1},(0.8 \mathrm{I}, 0.6,0.6 \mathrm{I})\right\rangle,\left\langle\mathrm{w}_{2},(, 0.6,0.7)\right\rangle,\left\langle\mathrm{w}_{3},(0.7 \mathrm{I}, 0.5,0.4)\right\rangle,\left\langle\mathrm{w}_{4},(0.3 \mathrm{I}, 0.5,0.5)\right\rangle\right)\right\}$.
$\mathrm{N} 1 \cap \mathrm{~N} 2=$

$$
\begin{aligned}
& \left\{\left(e_{1},\left\{\left\langle w_{1},(0.4 \mathrm{I}, 0.6,0.8)\right\rangle\left\langle\mathrm{w}_{2},(0.2,0.5 \mathrm{I}, 0.8)\right\rangle,\left\langle\mathrm{w}_{3},(0.3,0.1 \mathrm{I}, 0.5 \mathrm{I})\right\rangle,\left\langle\mathrm{w}_{4},(0.4 \mathrm{I}, 0.7,0.7 \mathrm{I})\right\rangle\right),\right.\right. \\
& \left(e_{2},\left\{\left\langle w_{1},(0.5 \mathrm{I}, 0.7 \mathrm{I}, 0.8)\right\rangle,\left\langle\mathrm{w}_{2},(0.3,0.9 \mathrm{I}, 0.3)\right\rangle,\left\langle\mathrm{w}_{3},(0.2 \mathrm{I}, 0.6,0.8)\right\rangle,\left\langle\mathrm{w}_{4},(0.4,0.8 \mathrm{I}, 0.5)\right\rangle\right),\right. \\
& \left(e_{3},\left\{\left\langle\mathrm{w}_{1},(0.7,0.8 \mathrm{I}, 0.9 \mathrm{I})\right\rangle,\left\langle\mathrm{w}_{2},(0.5,0.9 \mathrm{I}, 0.9)\right\rangle,\left\langle\mathrm{w}_{3},(0.7 \mathrm{I}, 0.5,0.8)\right\rangle,\left\langle\mathrm{w}_{4},(0.3 \mathrm{I}, 0.5,0.5)\right\rangle\right)\right\} .
\end{aligned}
$$

## 3 FUZZY NEUTROSOPHIC SOFT MATRICES

In this section, we have introduced fuzzy neutrosophic soft matrices (FNSM) and their operators which are more functional to make theoretical studies in the fuzzy neutrosophic soft set theory(FNSS). The matrix is useful for storing an FNSS in computer memory which are very useful and applicable. Some of its quoted from [1,2,13,20,26,37]. Throughout this section I is the indeterminable such that $\mathrm{I}^{2}=\mathrm{I}$.

Definition 3.1: Let A be a matrix if it entries are from $[0,1]$ and $[0,1]$ then we call $A$ to be a fuzzy neutrosophic soft matrix.

Example-1. Let $\mathrm{W}=\left\{\mathrm{w}_{1}, \mathrm{w}_{2}, \mathrm{w}_{3}\right\}, \mathrm{E}=\left\{\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}\right\}$. N be a fuzzy neutrosophic soft sets over neurosophic as $\mathrm{N}=\left\{\left(\mathrm{x}_{1},\left\{\left\langle\mathrm{w}_{1},(0.7,0.6 \mathrm{I}, 0.7\rangle,\left\langle\mathrm{w}_{2},(0.4 \mathrm{I}, 0.2,0.8)\right\rangle,\left\langle\mathrm{w}_{3},(0.9,0.1,0.5 \mathrm{I})\right\rangle\right\}\right.\right.\right.$,

$$
\begin{aligned}
& \left\{\left(\mathrm{x}_{2},\left\{\left\langle\mathrm{w}_{1},(0.5 \mathrm{I}, 0.7,0.8\rangle,\left\langle\mathrm{w}_{2},(0.5,0.9 \mathrm{I}, 0.3)\right\rangle,\left(\mathrm{w}_{3},(0.5,0.6 \mathrm{I}, 0.8)\right\rangle\right\},\right.\right.\right. \\
& \left\{\left(\mathrm{x}_{3},\left\{\left\langle\mathrm{w}_{1},(0.8 \mathrm{I}, 0.6,0.9\rangle,\left\langle\mathrm{w}_{2},(0.5,0.9 \mathrm{I}, 0.9)\right\rangle,\left(\mathrm{w}_{3},(0.7,0.5 .0 .4 \mathrm{I})\right\rangle\right\},\right.\right.\right.
\end{aligned}
$$

the FNSS-matrix [aij] is written by
$\left[\right.$ aij] $=\left[\begin{array}{lll}(0.7,0.6 \mathrm{I}, 0.7) & (0.4 \mathrm{I}, 0.2,0.8) & (0.9,0.1,0.5 \mathrm{I}) \\ (0.5 \mathrm{I}, 0.7,0.8) & (0.5,0.9 \mathrm{I}, 0.3) & (0.5,0.6 \mathrm{I}, 0.8) \\ (0.8 \mathrm{I}, 0.6,0.9) & (0.5,0.9 \mathrm{I}, 0.9) & (0.7,0.5 .0 .4 \mathrm{I})\end{array}\right]$

Definition 3.2: A fuzzy neutrosophic soft matrix FNSM of order $1 \times \mathrm{N}$. i.e., with a single row is called row fuzzy neutrosophic soft set matrix.

Example $\mathrm{N}=\left\{\mathrm{x}_{1},\left\{<\mathrm{w}_{1},(0.3,0.4 \mathrm{I}, 0.6)>\right\}\right),\left\{\left(\mathrm{x}_{2},<\mathrm{w}_{1},(0.3 \mathrm{I}, 0.2,0.3)>\right\},\left\{\left(\mathrm{x}_{3},<\mathrm{w} 3,(0.7,0.6,0.9 \mathrm{I})>\right\}\right.\right.$, then FNSM matrix [aij] is written by [aij ] = [ (0.3,0.4I, 0.6), (0.3I, 0.2, 0.3 ) , (0.7,0.6,0.9 I) ]

Definition 3.3:A fuzzy neutrosophic soft matrix (FNSM) of order $m \times 1 \quad$ i.e.) with a single column is called a column FNSM.

Example. In above example
$[$ aij $]=\left(\begin{array}{c}(0.3,0.4 \mathrm{I}, 0.6) \\ (0.3 \mathrm{I}, 0.2,0.3) \\ (0.7,0.6,0.9 \mathrm{I})\end{array}\right)$

Definition 3.4: A FNSM of order $\mathrm{m} \times \mathrm{n}$ is said to be a square FNSM if $\mathrm{m}=\mathrm{n}$. (i.e)., the number of rows and the number of columns are equal.

Example: Consider the example 1, Here since the FNSM contains three rows and three columns, so it is a square FNSM.

Definition 3.5: A square FNSM of order $\mathrm{m} \times \mathrm{n}$ is said to be a diagonal FNSM if all of its nondiagonal elements are $(0,0,1)$.

## Example:

$\left[\right.$ aij] $=\left[\begin{array}{lll}(0.7,0.6 \mathrm{I}, 0.7) & (0.0, \text { I.0, 1.0) } & (0.0,1.0, \mathrm{I} .0) \\ (0.0,1.0, \text { I.0) } & (0.0, \text { I.0, 1.0) } & (0.0,1.0 . \mathrm{I} .0) \\ (0.0, \text { I.0. 1.0) } & (0.0,1.0, \mathrm{I} .0) & (0.7 \mathrm{I}, 0.5 .0 .4)\end{array}\right]$

Definition 3.6: Let $\left[a_{i j}\right] \in N$, then $\left[a_{i j}\right]$ is called
(i) A Zero FNS-matrix, denoted by [ộ], if $\mathrm{a}_{\mathrm{ij}}=(0, \mathrm{I}, \mathrm{I})$ for all i and j .
(ii) A Universal FNS-matrix, denoted [ $[\hat{I}]$, if $\mathrm{a}_{\mathrm{ij}}=(\mathrm{I}, 0,0)$ for all I and j .

Example : Let $\mathrm{W}=\left\{\mathrm{w}_{1}, \mathrm{w}_{2}, \mathrm{w}_{3}\right\}, \mathrm{E}=\left\{\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}\right\}$, then a Zero FNS-matrix $\left[\mathrm{a}_{\mathrm{ij}}\right]$ is given by

$$
\left[\mathrm{a}_{\mathrm{ij}}\right]=\left[\begin{array}{lll}
(0, \mathrm{I}, \mathrm{I}) & (0, \mathrm{I}, \mathrm{I}) & (0, \mathrm{I}, \mathrm{I}) \\
(0, \mathrm{I}, \mathrm{I}) & (0, \mathrm{I}, \mathrm{I}) & (0, \mathrm{I}, \mathrm{I})
\end{array}\right]
$$

given by
$\left[\mathrm{a}_{\mathrm{ij}}\right]=\left(\begin{array}{lll}(\mathrm{I}, 0,0) & (\mathrm{I}, 0,0) & (\mathrm{I}, 0,0) \\ (\mathrm{I}, 0,0) & (\mathrm{I}, 0,0) & (\mathrm{I}, 0,0) \\ (\mathrm{I}, 0,0) & (\mathrm{I}, 0,0) & (\mathrm{I}, 0,0)\end{array}\right)$

Definition 3.7: Let $\left[a_{i j}\right],\left[b_{i k}\right] \in N$, then And-product of $\left[a_{i j}\right]$ and $\left[b_{i k}\right]$ is defined by
$\left[\mathrm{a}_{\mathrm{ij}}\right] \Lambda\left[\mathrm{b}_{\mathrm{ik}}\right]=\left[\mathrm{c}_{\mathrm{ip}}\right]$. Also max min product is defined by


## 4.Decision making problem using And-Product of fuzzy Neutrosophic soft matrices

## Algorithm-1(And-Product)

The algorithm for the solution is given below.
Step-1 Choose feasible subset of the set of parameters.

Step-2 Construct the fuzzy neutrosophic matrices for each parameter.
Step-3 Choose a And-product of the fuzzy neutrosophic matrices.

Step-4 Compare it and find the method min-max-max decision Fuzzy neutrosophic matrices.

Step-5 Find an optimum fuzzy set on X .

Case Study: Assume that a car dealer stores three different types of cars $\mathrm{W}=\left\{\mathrm{w}_{1}, \mathrm{w}_{2}, \mathrm{w}_{3}\right\}$ which may be characterize by the set of parameter $E=\left\{e_{1}, e_{2},\right\}$ where e1 stands for costly, $e_{2}$ stands for fuel efficiency, then we consider the following example. Suppose a couple Mr. X and Mrs. X come to the dealer to buy a car before Durga Pooja. If each partner has to consider his/her
own set of parameters., then we select the car on the basis of partner's parameters by using FNSmatrices as follows:

Step-1: First Mr. $X$ and Mrs. $X$ have to choose the sets of parameters $A=\left\{e_{1}, e_{2}\right\}$ and $B=\left\{e_{1}, e_{2}\right\}$ respectively.

Step-2: Then we construct the FNS-matrix [aij] and [bij] according to their set of parameters A and $B$ respectively as follows:
$[\mathrm{aij}]=\left(\begin{array}{ll}(0.2 \mathrm{I}, 0.3,0.4) & (0.1,0.4 \mathrm{I}, 0.5) \\ (0.3 \mathrm{I}, 0.5,0.1) \\ (0.1,0.6 \mathrm{I}, 0.3) & (0.7,0.6,0.2 \mathrm{I}) \\ (0.3,0.2 \mathrm{I}, 0.6)\end{array}\right)$
and
$[\mathrm{bij}]=\left(\begin{array}{ll}(0.5 \mathrm{I}, 0.6,0.3) & (0.2,0.5 \mathrm{I}, 0.3) \\ (0.2 \mathrm{I}, 0.7,0.3) & (0.3,0.5 \mathrm{I}, 0.2) \\ (0.3 \mathrm{I}, 0.7 \mathrm{I}, 0.2) & (0.3 \mathrm{I}, 0.6,0.7)\end{array}\right)$

Step 3: Now, we can find the And-Product of the FNS-matrics $\left[\mathrm{a}_{\mathrm{ij}}\right]$ and $\left[\mathrm{b}_{\mathrm{ij}}\right]$ as follows:
$\left[\mathrm{a}_{\mathrm{ij}}\right] \Lambda\left[\mathrm{b}_{\mathrm{ij}}\right]=\left(\begin{array}{llll}(0.2 \mathrm{I}, 0.6,0.3) & (0.2,0.5 \mathrm{I}, 0.3) & (0.1,0.6,0.3) & (0.1,0.5 \mathrm{I}, 0.3) \\ (0.2 \mathrm{I}, 0.7,0.1) & (0.3,0.5 \mathrm{I}, 0.1) & (0.2 \mathrm{I}, 0.7,0.2 \mathrm{I}) & (0.3,0.6,0.2 \mathrm{I}) \\ (0.1,0.7 \mathrm{I}, 0.2) & (0.1,0.6 \mathrm{I}, 0.3) & (0.3,0.7 \mathrm{I}, 0.2) & (0.3 \mathrm{I}, 0.6,0.6)\end{array}\right)$

Step4:To demonstrate, let us find $\mathrm{d}_{21}$ for $\mathrm{i}=2$.
Since $\mathrm{i}=2$ and $\mathrm{k} \in\{1,2\}$ so $\mathrm{d}_{21}=\left\{\mathrm{a}_{21}, \mathrm{~b}_{21}, \mathrm{c}_{21}\right\}$.
Let $\mathrm{t}_{2 \mathrm{k}}=\left\{\mathrm{t}_{21}, \mathrm{t}_{22}\right\}$, where $\mathrm{t}_{2 \mathrm{k}}=\left\{\mathrm{a}_{2 \mathrm{p}}, \mathrm{b}_{2 \mathrm{p}}, \mathrm{c}_{2 \mathrm{p}}\right\}$, then We have to find $\mathrm{t}_{2 \mathrm{k}}$ for all $\mathrm{k} \in\{1,2\}$.

First to find $t_{21} . I_{1}=\{p: 0 \leq p \leq 2\}$ for $k=1$ and $n=2$.

| We have $t_{21}$ | $=\left(\min \left\{a_{2 p}\right\}, \max \left(b_{2 p}\right\}, \max \left\{c_{2 p}\right\}\right)$ |
| ---: | :--- |
|  | $=\left(\min \left\{a_{21}, a_{22}\right\}, \max \left\{b_{21}, b_{22}\right\}, \max \left\{c_{21}, c_{22}\right\}\right)$ |
|  | $=(\min \{0.2 \mathrm{I}, 0.3\}, \max \{0.7,0.5 \mathrm{I}\}, \max \{0.1 .0 .1\})$ |
|  | $=(0.2 \mathrm{I}, 0.7,0.1)$ |
| [when $p=3,4] \quad \mathrm{t}_{22} \quad$ | $=\left(\min \left\{\mathrm{a}_{22}, a_{24}\right\}, \max \left\{\mathrm{b}_{23}, \mathrm{~b}_{24}\right\}, \max \left\{\mathrm{c}_{23}, \mathrm{c}_{24}\right\}\right)$ |
|  | $=(\min \{0.2 \mathrm{I}, 0.3\}, \max \{0.7,0.6\}, \max \{0.1 \mathrm{I}, 0.2 \mathrm{I}\})$ |
|  | $=(0.2 \mathrm{I}, 0.7,0.2 \mathrm{I})$ |

Similarly, we can find $d_{11}$ and $d_{31}$ as $d_{11}=(0.2 I, 0.6,0.3), d_{31}=(0.1,0.7 I, 0.3)$

Now, We calculate, for $\mathrm{i}=\{1,2,3\}$

$\operatorname{Max}\left(\mathrm{S}_{\mathrm{i}}\right)=\left(\begin{array}{l}0.02 \\ \mathbf{0 . 1 3} \\ 0.06 \mathrm{I}\end{array}\right)$ where $S_{i}=a_{11}--------------b_{11} X_{11}$

Step 5: Finally, we can find an optimum fuzzy set on $W$ as :
$\mathrm{OPT}_{\text {[dij] }}(\mathrm{X})=\left\{\mathrm{w}_{1} / 0.02, \mathbf{w}_{2} / \mathbf{0 . 1 3}, \mathrm{w}_{3} / 0.06 \mathrm{I}\right\}$, Thus $\mathrm{w}_{2}$ has the maximum value. Therefore the couple may decide to buy the car $\mathbf{w}_{\mathbf{2}}$.

The following max-min Product algorithm is also applicable to the above case study problems

## Algorithm 2 : [max-min product]

Step1: Choose feasible subset of the set of parameter.
Step 2: Construct the fuzzy neutrosophic matrices for each parameter.
Step 3: Choose a max-min product of the Fuzzy neurosophic soft matrix.
Step 4: Compare it and find the method min-max-max decision fuzzy neutrosophic matrices.
Step 5: Find an optimum fuzzy set on $X$.

Step-1: First Mr. X and Mrs. $X$ have to choose the sets of parameters $A=\left\{e_{1}, e_{2}\right\}$ and $B=\left\{e_{1}, e_{2}\right\}$ respectively.

Step-2: we construct the FNS-matrix [aij] and [bij] according to their set of parameters A and B respectively as follows:
$\left[\mathrm{a}_{\mathrm{ij}}\right]=$
$\left[\mathrm{b}_{\mathrm{ij}}\right]=$
$\left(\begin{array}{lll}(0.2 \mathrm{I}, 0.3,0.4) & (0.1,0.4 \mathrm{I}, 0.5) & (0.3,0.5 \mathrm{I}, 0.6) \\ (0.3 \mathrm{I}, 0.5,0.1) & (0.7,0.6,0.2 \mathrm{I}) & (0.4 \mathrm{I}, 0.2,0.1 \mathrm{I}) \\ (0.1,0.6 \mathrm{I}, 0.3) & (0.3,0.2 \mathrm{I}, 0.6) & (0.6 \mathrm{I}, 0.3,0.7 \mathrm{I})\end{array}\right)$
$\left(\begin{array}{ll}(0.5 \mathrm{I}, 0.6,0.3) & (0.2,0.5 \mathrm{I}, 0.3) \\ (0.3 \mathrm{I}, 0.7,0.3) & (0.3,0.5 \mathrm{I}, 0.2)\end{array}\right.$

International Journal of Engineering, Science and Mathematics http://www.ijmra.us

Step 3: Now, we can find the max-min product of the FNS-matrices $\left[\mathrm{a}_{\mathrm{ij}}\right]$ and $\left[\mathrm{b}_{\mathrm{ij}}\right]$ as follows
$\left[\mathrm{a}_{\mathrm{ij}}\right] \circ\left[\mathrm{b}_{\mathrm{ij}}\right]=\left(\begin{array}{ll}(0.3,0.5 \mathrm{I}, 0.3) & (0.3,0.5 \mathrm{I}, 0.6) \\ (0.3,0.6,0.2 \mathrm{I}) & (0.3,0.5 \mathrm{I}, 0.2) \\ (0.3,0.6 \mathrm{I}, 0.3) & (0.3,0.5 \mathrm{I}, 0.7 \mathrm{I})\end{array}\right)$

Step 4: min-max-max decision fuzzy neutrosophic soft matrix
$\left[\mathrm{d}_{\mathrm{ij}}\right]=\left(\begin{array}{ll}(0.3, & 0.5 \mathrm{I}, \\ (0.6) \\ (0.3, & 0.6, \\ 0.2 \mathrm{I}) \\ (0.3, & 0.6 \mathrm{I}, \\ 0.7 \mathrm{I})\end{array}\right)$
$\operatorname{Max}(\mathrm{Si})=0.00$
$\left(\begin{array}{c}0.18 \mathrm{I} \\ \\ -0.12 \mathrm{I}\end{array}\right)$ where $S_{i}=a_{11}-\ldots------b_{11} \times c_{11}$
Step 5: Finally, we can find an optimum fuzzy set on W.

Thus $\mathrm{W}_{2}$ has the maximum value, then for the couple my decide to buy the car $\mathrm{W}_{2}$.
Among the above two different algorithms, they have the maximum value in the same position, but in second algorithm one value of the optimum fuzzy set is negative. So Algorithm -1 is most suitable than max-min product.
5.Conclusion: In this paper, we have introduced the notion of neutrosophic at in a new way and proposed the concept of FNS-matrix called max-min product and And - Product of matrix has been defined, then we discuss the group decision value problem under certain algorithm.

## References

[1] A.Q. Ansaria, R. Biswasb and S. Aggarwalc, Neutrosophic classifier: An extension of fuzzy classifer, Applied Soft Computing 13 (2013) 563-573.
[2] C. Ashbacher, Introduction to Neutrosophic Logic, American Research Press Rehoboth 2002.
[3] K. Atanassov, G. Gargov, Interval valued intuitionistic fuzzy sets, Fuzzy Sets Syst. 31 (1989) 343-349.23
[4] K.T. Atanassov, Intuitionistic Fuzzy Sets, Pysica-Verlag A Springer-Verlag Company, New York (1999).
[5] T. M. Basu, N. K. Mahapatra and S. K. Mondal, Intuitionistic Fuzzy Soft Matrix and Its Application in Decision Making Problems, Annals of Fuzzy Mathematics and Informatics x/x, (201y), pp.
[6] M. J. Borah, T. J. Neog, D. K. Sut, Fuzzy Soft Matrix Theory And Its Decision Making, International Journal of Modern Engineering Research, 2 (2012) 121-127.
[7] S. Broumi, Generalized Neutrosophic Soft Set International Journal of Computer Science, Engineering and Information Technology (IJCSEIT),/2, 2013.
[8] S. Broumi, F. Smarandache, Intuitionistic Neutrosophic Soft Set, Journal of Information and Computing Science 8/2, (2013), 130-140.
[9] S. Broumi, F. Smarandache and M. Dhar, On Fuzzy Soft Matrix Based on Reference Function, Information Engineering and Electronic Business,2 (2013) 52-59.
[10] S.Broumi,I.Deli,F.Smarandache," Relation on Interval Neutrosophic Soft Set", Journal of New Results in Science, 2014,submitted.
[11] Chetia, B. and Das,P.K.,An application of intuitionistic fuzzy soft matrices in decision making problems (communicated)
[12] N.Cagman and S. Engino glu, Soft matrix theory and its decision making, Computers and Mathematics with Applications 59 (2010) 3308-3314.
[13] N.Cagman, Contributions to the theory of soft sets, Journal of New Results in Science, 4 (2014), 33-41.
[14] N.Cagman and S. Enginolu, Fuzzy soft matrix theory and its applications in decision making, Iranian Journal of Fuzzy Systems, 9/1 (2012)109-119.
[15] N.Cagman, S. Karata ${ }_{s}$ s, Intuitionistic fuzzy soft set theory and its decision making, Journal of Intelligent and Fuzzy Systems 24/4 (2013) 829-836.
[16] Cagman, N. Deli, I. Means of FP-Soft Sets and its Applications, Hacettepe Journal of Mathematics and Statistics, 41/5 (2012) 615-625.
[17] Cagman, N. Deli, I. Product of FP-Soft Sets and its Applications, Hacettepe Journal of Mathematics and Statistics 41/3 (2012) 365-374.
[18]Deli,I."Interval-valued neutrosophic soft sets and its decision making",http://arxiv.org/abs/1402.3130
[19] I .Deli,. S.Broumi ,"neutrosophic soft relation" (communicated)
[20] B. Dinda and T.K. Samanta, Relations on Intuitionistic Fuzzy Soft Sets, Gen. Math. Notes, 1/2 (2010) 74-83.
[21] F. Feng, X. Liu , V. L. Fotea, Y. B. Jun, Soft sets and soft rough sets, Information Sciences 181 (2011) 1125-1137.
[22] W.L. Gau, D.J. Buehrer, Vague sets, IEEE Trans. Systems Man and Cy-bernet, 23 (1993), 610-614.
[23] A. Kalaichelvi, P. Kanimozhi, Impact of excessve television Viewing by children an analysis using intuitionistic fuzzy soft Matrices, International journal of mathematical sciences and applications 3/1 (2013) 103-108.
[24] Z. Kong, L. Gao and L. Wang, Comment on "A fuzzy soft set theoretic approach to decision making problems", J. Comput. Appl. Math. 223(2009) 540-542.
[25] P.K. Maji, R.Biswas A.R. Roy, Intuitionistic Fuzzy Soft Sets. The Journal of Fuzzy Mathematics, 9(3) (2001) 677-692.
[26] P.K. Maji, Neutrosophic soft set, Computers and Mathematics with Applications, 45 (2013) 555-562.
[27] P.K. Maji, A neutrosophic soft set approach to a decision making problem, Annals of Fuzzy Mathematics and Informatics, 3/2, (2012), 313-319.
[28] P.K. Maji, R. Biswas and A.R. Roy, Fuzzy soft sets, Journal of Fuzzy Mathematics, 9(3) (2001) 589-602.
[29] J. Mao, D. Yao, C. Wang, Group decision making methods based on intuitionistic fuzzy soft matrices, Applied Mathematical Modelling 37(2013) 6425-6436.
[30] J. I. Mondal and T. K. Roy, Some Properties on Intuitionistic Fuzzy Soft Matrices, International Journal of Mathematics Research 5/2 (2013)267-276.
[31] J. I. Mondal and T. K. Roy, Intuitionistic Fuzzy Soft Matrix Theory and Multi Criteria in Decision Making Based on T-Norm Operators, Mathematics and Statistics 2/2 (2014) 55-61.
[32] J. I. Mondal, T. K. Roy, Theory of Fuzzy Soft Matrix and its Multi Criteria in Decision
Making Based on Three Basic t-Norm Operators, International Journal of Innovative Research in Science, Engineering and Technology 2/10 (2013) 5715-5723.
[33] D.A. Molodtsov, Soft set theory-first results, Comput. Math. Appl. 37 (1999) 19-31.26
[34] Z. Pawlak, Rough sets, Int. J. Comput. Inform. Sci. 11 (1982) 341-356.
[35] D. Rabounski F. Smarandache L. Borissova Neutrosophic Methods in General Relativity, Hexis, 2005 no:10.
[36] A.R. Roy and P.K. Maji, A fuzzy soft set theoretic approach to decision making problems, J. Comput. Appl. Math. 203 (2007) 412-418.
[37] F.Smarandache,"A Unifying Field in Logics. Neutrosophy: Neutrosophic Probability, Set and Logic". Rehoboth: American Research Press,(1998).
[38] B.K. Saikia, H. Boruah and P.K. Das, Application of Intuitionistic Fuzzy Soft Matrices in Decision Making Problems, International Journal of Mathematics Trends and Technology, 4/11 (2013) 254-265.
[39] B.K. Saikia, H. Boruah and P.K. Das, An Appliaction of Generalized Fuzzy Soft Matrices in Decision Making Problem, IOSR Journal of Mathematics, 10/1 (2014), PP 33-41.
[40] A. Sezgin and A.O. Atag"un, On operations of soft sets, Computers and Mathematics with Applications, 61/5 (2011) 1457-1467.
[41] T. Som, On the theory of soft sets, soft relation and fuzzy soft relation, Proc. of the national conference on Uncertainty: A Mathematical Approach, UAMA-06, Burdwan, 2006, 1-9.
[42] D. K. Sut, An application of fuzzy soft relation in decision making problems, International Journal of Mathematics Trends and Technology 3/2(2012) 51-54.27
[43] H. Wang, F. Smarandache, Y.Q. Zhang, R. Sunder raman, Interval Neutrosophic Sets and Logic: Theory and Applications in Computing, Hexis; Neutrosophic book series, No: 5, 2005.
[44] L.A. Zadeh, Fuzzy Sets, Inform. and Control 8 (1965) 338-353.


[^0]:    * Associate Professor, Department of Mathematics, J.J College of Engineering \&Technology, Tiruchirappalli-09

